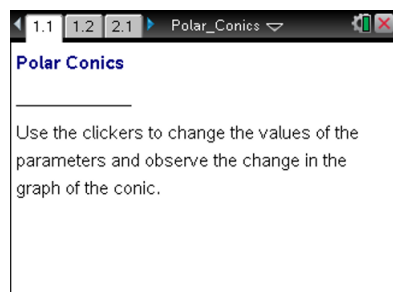




Open the TI-Nspire document *Polar_Conics.tns*.

In this activity, you will explore how to express an ellipse, a hyperbola, and a parabola from a single equation and investigate the different parameters of the equation.



A conic is defined as the locus of points in a plane whose distance from a fixed point (focus) and a fixed line (directrix) is a constant ratio. This ratio is called the eccentricity, e , of the conic. The polar notation for the ellipse, hyperbola, and parabola is given by the equation:

$$r = \frac{ed}{1 \pm e \cos(\theta)} \text{ OR } r = \frac{ed}{1 \pm e \sin(\theta)}$$

where e is the eccentricity and d is the distance from the origin to the directrix.

By expressing the equation in polar coordinates, we can generate all three types of conics from a single equation.

Move to page 1.2.

Press **ctrl** **▶** and **ctrl** **◀** to
navigate through the lesson.

1. Use the clicker to change the values of the eccentricity, e . For what values of e is the conic a parabola? An ellipse? A hyperbola?

Move to page 2.2.

2. Use the clicker to change the values of d , the distance between a point on the conic and the directrix.
 - a. Set $e = 1$. When the conic is a parabola, what effect does d have on the graph of the function?
 - b. Set $e < 1$. When the conic is an ellipse, what effect does d have on the graph of the function?
 - c. When the conic is a hyperbola, what effect does d have on the graph of the function?



3. Adjust the parameters to create an ellipse that is 9 units in width, and make a note of those parameters. Are these the only parameters that will create such an ellipse? Explain.

4. Adjust the parameters to create a hyperbola for which the vertices of the branches are 6 units apart, and make a note of those parameters. Are these the only parameters that will create such a hyperbola? Explain.

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5. Use the clicker to adjust the value of a , the phase shift.
 - a. Set $e = 1$. When the conic is a parabola, what effect does a have on the graph of the function?

 - b. Set $e < 1$. When the conic is an ellipse, what effect does a have on the graph of the function?

 - c. Set $e > 1$. When the conic is a hyperbola, what effect does a have on the graph of the function?

6. Is it possible to adjust the values of a and e so that the resulting conic is a parabola centered about the y -axis? If so, what parameters yield this result? If not, explain why not.

7. Which type of conic will result from each of the following equations? How do you know?
 - a. $r = \frac{10}{1+3 \cos(\theta-5)}$

 - b. $r = \frac{2}{1-\cos(\theta-6)}$

 - c. $r = \frac{20}{1-0.5 \cos(\theta-2)}$